A NOTE ON THE HERMITE NUMBERS AND POLYNOMIALS

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Abstract. In this paper, we compute explicitly an integral involving the Hermite polynomials. From our computation, we derive the formula for a product of two Hermite polynomials. Finally, we give some interesting formulae for the product of two Hermite polynomials associated with Bernoulli polynomials like Carlitz did.

Mathematics subject classification (2010): 11B68, 33C45.
Keywords and phrases: Hermite polynomials, Bernoulli polynomials.

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