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# The Classical Umbral Calculus

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A rigorous presentation of the umbral calculus, as formerly applied heuristically by Blissard, Bell, Riordan, and others is given. As an application, the basic identities for Bernoulli numbers, as well as their generalizations first developed by Nörlund are derived.

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